

# 國立中央大學八十八學年度碩士班研究生入學試題卷

所別： 應用地質研究所 不分組 科目： 微積分 共一頁 第一頁

- 1) If  $f(x) = x^n$ , where  $n$  is a positive integer, then  $f'(x) = nx^{n-1}$  and find  $f'(-1)$  if  $f(x) = x^9$ . 10%
- 2) Evaluate  $\lim_{t \rightarrow 0} \left( \frac{t^2 + 1}{t} \right) \sin(t)$  and  $\lim_{x \rightarrow 0} \frac{x}{1 + \sin x}$ . 10%
- 3) Find  $\int_1^3 (2x^2 - 5) dx$  and  $\int_1^2 \sqrt{3 + 2t - t^2} dt$ . 10%
- 4) Find  $\int_0^4 \frac{1}{\sqrt{x}} dx$  and  $\int_{-1}^8 x^{-2/3} dx$ . 10%
- 5) Find the area of the region bounded by the  $x$ -axis, the line  $x=2$ , and the graph of  $f(x) = x^3 - 2x^2 + 3$ . 10%
- 6) Find the volume generated when the region bounded on  $[-1, 0]$  by the  $x$ -axis and the graph of  $y = x^2 + 1$  is revolved about the line  $y = 2$ . 10%
- 7) Show that  $\lim_{x \rightarrow \infty} \left(1 + \frac{1}{x}\right)^x = e$  and  $e^x = \sum_{n=0}^{\infty} \frac{x^n}{n!}$ . 10%
- 8) Determine  $\iint_S z d\sigma$ , where  $S$  is described by  $z = \sqrt{4 - x^2 - y^2}$ . 10%
- 9) Solve the following differential equations. 20%
  - a)  $\frac{dy}{dx} + y = xy^3$
  - b)  $y'' - 4y' + 4y = e^x \sin(x)$  with the condition  $y(0) = 0$ ,  $y'(0) = 0$ .

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