

國立中央大學八十七學年度碩士班研究生入學試題卷

所別：應用地質研究所 不分組 科目：

微積分

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- 1) Show that if $\tan y = x$ and $-\pi/2 < y < \pi/2$, then

$$\frac{dy}{dx} = \frac{1}{1+x^2}$$

10%

- 2) Evaluate $\lim_{x \rightarrow \frac{\pi}{2}^-} \frac{2x + \sec x}{3 + \tan x}$ and $\lim_{x \rightarrow 0^+} (\csc x - \cot x)$.

12%

- 3) Find $\int_0^1 x \sqrt{x+1} dx$ and $\int_{-1}^1 \frac{1}{x^3} dx$

12%

- 4) Find $\int_2^4 \frac{\sqrt{x^2 - 4}}{x} dx$ and $\int \frac{x^2 + 3x + 3}{x(x+2)^2} dx$.

12%

- 5) An outdoor thermometer reading $\sim 3^\circ C$ is into a $20^\circ C$ room.
One minute later the thermometer reads $5^\circ C$. How long will
it take to reach $19.5^\circ C$? 12%

- 6) Find the length of the spiral $r = e^{\theta/2\pi}$ for the range $-2\pi \leq \theta \leq 0$. 12%

- 7) Evaluate $\int_0^2 \int_0^{\sqrt{4-x^2}} e^{-x^2} e^{-y^2} dy dx$ 10%

- 8) Find the maximum and minimum values of $f(x,y,z) = 2x - 2y + z$
for (x,y,z) lying on the sphere $x^2 + y^2 + z^2 = 9$. 10%

- 9) Solve the differential equation $y''' - 5y' + 6y = 0$. 10%