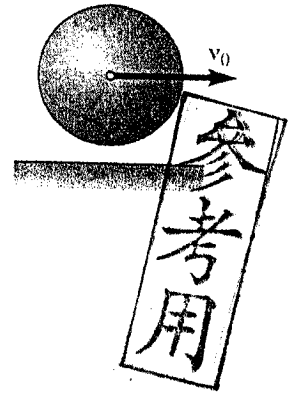
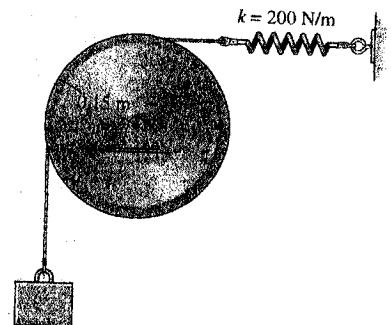


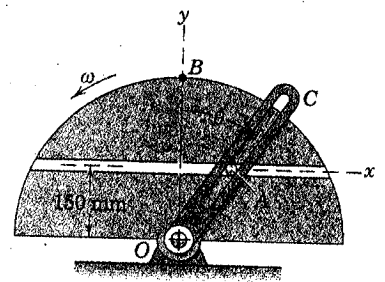
1. (25%) A uniform sphere of mass  $m$  and radius  $r$  is projected along a rough horizontal surface with a linear velocity  $v_0$  and no angular velocity. Denoting by  $\mu_k$  the coefficient of kinetic friction between the sphere and the floor, determine (a) the time  $t_f$  at which the sphere will roll without sliding, (b) the linear velocity and angular velocity of the sphere at time  $t_f$ .



2. (25%) A 10-kg block is suspended from a cord wrapped around a 5-kg disk. If the spring has a stiffness  $k = 200 \text{ N/m}$ , determine the natural period of vibration for the system.



3. (25%) The slotted disk sector rotates with a constant counterclockwise angular velocity  $\omega = 3 \text{ rad/s}$ . Simultaneously the slotted arm  $OC$  rotates about the  $y$  axis so that  $\theta$  changes at the constant rate of  $2 \text{ rad/s}$ . Find the acceleration of the pin  $A$  when  $\theta = 30^\circ$  and  $\dot{\theta}$  is positive (clockwise).



4. (25%) Two men  $A$  and  $B$ , each having a weight of  $80 \text{ kgf}$ , stand on the  $240\text{-kg}$  raft. Each can run with a speed of  $2 \text{ m/s}$  measured relative to the raft. Turning of the raft and water resistance are neglected.

- (a) Please determine the final speed of the raft if  $A$  runs and jumps off, then  $B$  runs and jumps off. (10%)  
 (b) Please also determine the final speed of the raft if both run at the same time and jump off. (10%)  
 (c) Besides, please discuss in brief how you deal with above two problems! (5%)

