## 台灣聯合大學系統102學年度碩士班招生考試命題紙 共了頁第一頁

科目: 物理化學(1004)

校系所組:中央大學化學學系

交通大學應用化學系(甲組)

清華大學化學系

清華大學材料科學工程學系(丙組)

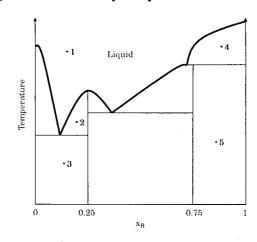
- 1. (15 %) Calculate the work, heat, energy, enthalpy, entropy, and Gibbs free energy of one mole ideal gas that undergoes reversible isothermal compression from V to V/2.
- 2. (10 %) Starting with the virial equation for a real gas in the following form

$$PV_m = RT \times (1 + \frac{B(T)}{V_m})$$

 $V_m$  and B(T) represent the molar volume and temperature-dependent virial coefficient, respectively. If the sample undergoes isothermal expansion from V to 2V,

(1) Derive "X" and "Y" for 
$$\left(\frac{\partial H}{\partial V}\right)_T = X \left(\frac{\partial P}{\partial V}\right)_T + Y \left(\frac{\partial P}{\partial T}\right)_V$$
. (4 %)

- (2) Derive  $\left(\frac{\partial H}{\partial V}\right)_T$  in terms of B, T, V, R, and  $\frac{\partial B}{\partial T}$  . (3 %)
- (3) Derive the molar enthalpy change ( $\Delta H_m$ ). (3 %)
- 3. (9 %) A phase diagram for the binary alloy A+B is shown below.



x<sub>B</sub> represents the molar fraction of component B. Please answer the questions (a)-(c).

Point	Composition
1	Liquid
2	(a)
3	(b)
4	(c)
5	Pure $B_{(s)} + AB_{3(s)}$

注:背面有試題

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4. (8%) A hypothetical chain reaction leads to a complicated rate law.

$$A_2 + B_2 \rightarrow 2 AB$$
 
$$\frac{d[AB]}{dt} = \frac{k_1[A_2][B_2]^{3/2}}{[B_2] + k_2[AB]}$$

The reaction mechanism is defined as a proposed set of elementary steps:

Initiation: 
$$B_2 + M \xrightarrow{k_a} B + B + M \xrightarrow{\frac{1}{2}} \frac{d[B]}{dt} = k_a[M][B_2]$$

Propagation: B + A<sub>2</sub> 
$$\xrightarrow{k_b} AB + A$$
  $\xrightarrow{d[AB]} k_b[A_2][B]$ 

$$A + B_2 \xrightarrow{k_c} AB + B \quad \frac{d[AB]}{dt} = k_c[A][B_2]$$

Inhibition: 
$$A + AB \xrightarrow{k_d} A_2 + B \xrightarrow{d[AB]} = -k_d[A][AB]$$

Termination: B + B + M 
$$\stackrel{k_e}{\rightarrow} B_2 + M$$
  $\frac{1}{2} \frac{d[B]}{dt} = -k_e[B]^2[M]$ 

Derive  $k_1$  and  $k_2$  in terms of  $k_a$ ,  $k_b$ ,  $k_c$ ,  $k_d$ , and  $k_e$  when applying the steady-state approximation on d[A]/dt and d[B]/dt.

5. (8%) A reversible reaction is expressed in the following form

$$A \stackrel{k_f}{\underset{k_r}{\rightleftarrows}} B$$
.

The initial concentrations of A and B are  $[A]_0$  and 0, respectively.  $k_f$  and  $k_r$  represent the first-order rate coefficients of the forward and backward reactions, respectively.

- (1) Derive the time dependence of [A] and [B]. (4 %)
- (2) Derive the concentrations of [A] and [B] at equilibrium. (4%)
- 6. (10%) Explain the method of using half-life times to derive the order of a chemical reaction for the 0-, 1st-, and 2nd-order reaction. Please write down the proper equation to describe your method.
- 7. (5%) For the gas-phase reaction  $H_2 + Br_2 \rightarrow 2HBr$  at 373.15 K, the rate constant is equal to  $8.75 \times 10^{-15} \, \text{L mol}^{-1} \, \text{s}^{-1}$ . At 473.15 K it is equal to  $9.53 \times 10^{-15} \, \text{L mol}^{-1} \, \text{s}^{-1}$ . Show all the details for how to find the value of the activation energy and of the preexponential factor.



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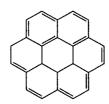
清華大學化學系

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8. (7%) For (1) B<sub>2</sub>, and (2)H<sub>2</sub>O<sub>2</sub> molecules, determine (a) the point group, (b) the term symbol of ground state, (c) whether it has a permanent dipole moment, (d) whether it is optically active, (e) whether it is microwave spectrum active.

- 9. (20%) The partition function is the fundamental concept of statistical thermodynamics.
  - (1) For an ideal gas, define the molar partition function, Q, by partition function of one partical, q.
  - (2) The Hamiltonian of an individual molecule can be simplified based on Born-Oppenheimer approximation. What is the Born-Oppenheimer approximation?
  - (3) Describe the result of the simplified Hamiltonian based on Born-Oppenheimer approximation.
  - (4) For each part of (3) state a proper model to botain the eigenvalues, *i.e.*, energy levles.
  - (5) What is the partition function of a molecule, q? Express it with degneracy and energy level. (You do not have to do the summation or integration.)

## 10. (8%) The molecule cocronen



is quite often used as a very simple modle of graphene. Show how you will calcualte the frequency of the  $\pi$  electron transition. The carbon-carbon distance is 1.33Å.

