

科目：訊號與系統(300C)

校系所組：中央大學電機工程學系(電子組)

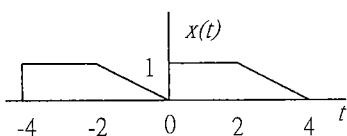
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1. For signal $x(t)$ depicted below, sketch and label carefully each of the following signals.

(a) $x\left(\frac{t}{2}-2\right)$ (2%)

(b) even signal of $x(t)$ (3%)



2. Consider an LTI system with input and output related through the equation $y(t) = \int_{-\infty}^t e^{-(t-\tau)} x(\tau-1) d\tau$

Find the impulse response $h(t)$ for this system. (5%)

3. Consider the LTI system initially at rest and described by the difference equation

$$y[n] + 2y[n-1] = x[n] + 2x[n-2]$$

Find the response of this system to the input $x[n] = \delta[n+2] + 2\delta[n+1] + 3\delta[n] + 2\delta[n-1] + 2\delta[n-2]$ (5%)

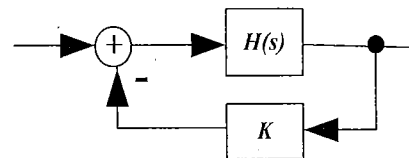
4. $X(s) = \frac{2s-1}{s^3-s}$, determine

(a) $x(t)$ (5%)

(b) the initial and final values of $x(t)$. (5%)

5. Consider a feedback system shown below, where $H(s) = \frac{s+2}{s^2+2s+4}$

(a) Find the smallest positive value of K for which the closed-loop impulse response doesn't exhibit any oscillatory behavior. (5%)



(b) Find the value of K for which the phase margin is $\frac{\pi}{3}$. (5%)

(c) Find the value of K for which the closed-loop damping factor is $\frac{1}{\sqrt{2}}$. (5%)

6. Consider the following system.



(a) Let $H(z) = \frac{1-\frac{2}{9}z^{-1}}{1-\frac{1}{3}z^{-1}}$ and $x[n] = \left(\frac{1}{6}\right)^n u[n]$, where $u[n]$ is the unit step function with unity gain for $n \geq 0$. If Region of Convergence (ROC) of $y[n]$ is a ring, determine the output $y[n]$. (5%)

(b) Let $H(z) = \frac{1-2\sqrt{2}z^{-1}}{1-\frac{\sqrt{2}}{3}z^{-1}}$ and $x[n] = \frac{1}{6} [\sin \Omega_0 n] u[n]$ for $\Omega_0 = \frac{\pi}{4}$. If ROC of $y[n]$ exists, determine the output $y[n]$? (10%)

7. Let $x(t) = \cos(4\pi f_2 t) e^{j2\pi f_1 t}$ and $f_2 > f_1 > 0$.

(a) What is the criterion for sampling frequency f_s (Nyquist frequency)? (3%)

(b) If $y(t) = (x(t))^2$, what is the criterion for sampling frequency f_s (Nyquist frequency)? (3%)

(c) If $y_p(t) = y(t)p(t)$ and $p(t) = \sum_{n=-\infty}^{+\infty} \delta\left(t - \frac{n}{12f_2}\right)$, please depict the spectrum $Y_p(\omega)$ of $y_p(t)$ with y-axis indicating the magnitude of $|Y_p(\omega)|$. (5%)

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(d) If an ideal low-pass filter with cutoff frequency ω_c is used to interpolate $y_p(t)$ for reconstructing $y(t)$, what is the requirement for ω_c without generating the aliasing effect? (4%)

8. Suppose that a continuous-time periodic signal $x(t)$ is the input to an LTI system. The signal has a Fourier series representation: $x(t) = \sum_{k=-\infty}^{\infty} \alpha^{|k|} e^{jk(\pi/4)t}$, where α is a real number and $0 < \alpha < 1$, and the frequency response of the system is

$$H(j\omega) = \begin{cases} 1, & |\omega| \leq W \\ 0, & |\omega| > W \end{cases}$$

(a) The fundamental period of $x(t) =$ _____. (2%)

(b) The average energy per period of $x(t) =$ _____. (3%) (express the average energy per period in terms of α)

(c) For the output of the system to have at least 90% of the average energy per period of $x(t)$, the frequency $W =$ _____. (5%) (express W in terms of α)

You need to write down your answers only. No partial scores for your computation procedures.

9. Consider a continuous-time system with frequency response $H(j\omega)$ shown below.

(a) The energy of the impulse response $h(t)$ of the system = _____. (3%)

(b) When the input of the system is given by $x(t) = 2(\cos 2t)(\sin 7t)$, the output

$y(t) =$ _____. (3%)

(c) When the input is an impulse train given by $x(t) = \sum_{k=-\infty}^{\infty} \delta(t - k - 1)$, the output $y(t)$ computed by first

finding out $Y(j\omega) = H(j\omega)X(j\omega)$ then obtaining $y(t)$ from $Y(j\omega) =$ _____. (4%)

(Note: Direct convolution of $x(t)$ and $h(t)$ to obtain $y(t)$ will get no credit.)

You need to write down your answers only. No partial scores for your computation procedures.

10. When the impulse train $x[n] = \sum_{k=-\infty}^{\infty} \delta[n - 4k - 1]$ is the input to a particular LTI system with frequency

response $H(e^{j\omega})$, the output of the system is found to be $y[n] = \cos(\frac{5\pi}{2}n + \frac{\pi}{4})$.

(a) The value of $H(e^{j0}) =$ _____. (3%)

(b) $\sum_{k=0}^3 H(e^{jk\pi/2}) =$ _____. (7%)

You need to write down your answers only. No partial scores for your computation procedures.

