

所別：光電科學研究所碩士班 一般生 科目：電磁學
學位在職生

(共八大題，每大題 12.5 分，總分 100 分)

1. An electric dipole $\mathbf{p}_1 = p_1 \mathbf{e}_z$ is located at the origin of the coordinate system. A second dipole $\mathbf{p}_2 = p_2 \mathbf{e}_z$ is located at (a) on the $+z$ axis a distance r from the origin, or (b) on the $+y$ axis a distance r from the origin. Show that the force between the two dipoles is attractive in case (a) and repulsive in case (b).
2. A conducting sphere with total charge Q is cut into half. What force must be used to hold the two halves together?
3. Two uniform infinite sheets of electric charge densities $+\sigma$ and $-\sigma$ intersect at right angles. Find the magnitude and direction of the electric field everywhere and sketch the lines of \mathbf{E} .
4. Two infinite current sheets, each of current density K_0 , are parallel and have their currents oppositely directed. Find the force per unit area on the sheets. Is the force repulsive or attractive?
5. A) When a light wave is incident from one medium to another one, and if I want to find the phases of the reflected and transmitted waves in terms of that of the incident wave, I should use which of the following equations:
 - a) Maxwell equations
 - b) The wave equation
 - c) Fresnel equations
 - d) Snell's law

Just choose the answer you think that is right and write it down on the answer sheet. You don't need to give reason.

B) Snell's law results from

- a) Coulomb's law
- b) Faraday's law
- c) Maxwell equations
- d) The continuity of the tangential components of \mathbf{E} and of \mathbf{H} at the interface between 2 dielectric media.

Just tell me which one is the most appropriate answer. You don't have to give reason.

注意：背面有試題

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- C) For a wave guide made of infinitely conducting material, show that the tangential component of the \mathbf{E} field at the inner surface of the guide is zero.
6. For a wave guide made of infinitely conducting material,
- Must the normal components of the \mathbf{E} field to the guide wall be zero at the inner surface?
 - Show that the \mathbf{H} field must lie on the guide wall at the inner surface.
 - Show that the tangential component of \mathbf{H} at the inner surface is perpendicular to the current density in the guide wall.
 - Show that the tangential component of \mathbf{H} at the inner surface is equal to the current density in magnitude expressed in amperes/meter.
7. a) Show that the phase velocity of a plane wave propagating in z -direction such as $\mathbf{E}_0 \cos(\omega t - kz)$ is ω/k . Explain your mathematical steps with words clearly.
- b) Given that the relative permittivity ϵ_r and relative permeability μ_r of a material are 2 and 1.1, respectively. Find the wave length of a beam of light wave whose frequency is 10^{14} Hz propagating in it
8. a) Consider an optical plane wave incident normally upon a perfectly conducting material. Show that it is 100% reflected from it, and the phase of the incident wave and the reflected wave is reverse to each other.
- b) Is there any charge induced on the surface of the perfectly conducting material?