

中央大學八十九學年度碩士班研究生入學試

應用地質研究所 不分組 科目:

微積分

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1) Sketch the graph of $f(x)=2x^2+12x+17$ and $f(x)=x^2-3x^{\frac{2}{3}}$ 10%

2) Show that (a) if $f(x)=\tan x$, then $f'(x)=\sec^2 x$ and (b) $f(x)=a^x$,

then $f'(x)=a^x \log a$. 10%

3) Evaluate $\lim_{x \rightarrow 9} \frac{\sqrt{x}-3}{x-9}$ and $\lim_{x \rightarrow 0} \frac{x}{1+\sin x}$ 10%

4) Find $\int \frac{x+1}{\sqrt{x^2+2x}} dx$ and $\int_0^1 x\sqrt{x+1} dx$ 10%

5) Suppose S is a cone lying between the planes that pass through $x=0$ and $x=6$ that every cross section of S perpendicular to the x -axis is a circle with radius $x/2$. Find the volume of S. 10%

6) Show that $e^x = \sum_{n=0}^{\infty} \frac{x^n}{n!}$ and find $\sum_{n=1}^{\infty} \frac{1}{n(n+1)}$ 10%

7) Find the length of the cardioid $r=2(1+\cos \theta)$ 10%

8) Evaluate $\int_0^1 \int_x^1 e^{y^2} dy dx$ and $\int_0^2 \int_0^{\sqrt{4-x^2}} e^{-x^2} e^{-y^2} dy dx$ 15%

9) Find a particular solution to

$$y'' - y' - 2y = e^x - 2x^2 \quad 15\%$$