

所別：大氣物理研究所碩士班 一般生 科目：流體力學

1. Provide a physical interpretation and list the assumptions that must be satisfied for the different forms of Bernoulli's equation to be valid. (10 %)

2. A fluid whose density distribution is given by  $\rho(Z) = \rho_H - (\rho_B - \rho_H) \left[ \left( \frac{Z}{H} \right)^2 - 1 \right]$

is at rest in Earth's gravity field, where  $\rho_H, \rho_B$  are constant. Find the pressure gradient acting in the fluid at a depth of  $2H/3$ . (10 %)

3. Provide a physical interpretation of Reynolds transport theorem as applied to a system and a control volume. (10 %)

4. The velocity field for a flow is given by  $\vec{u} = \frac{-C \cdot y}{\sqrt{x^2 + y^2}} \hat{i} + \frac{C \cdot x}{\sqrt{x^2 + y^2}} \hat{j}$

where C is a constant. Determine the equations for the streamlines and make a sketch. (10 %)

5. Given the velocity field  $\vec{v} = (x^2 - y^2) \hat{i} - 2xy \hat{j}$

(1) determine the velocity gradient (5 %)

(2) determine the vorticity field (5 %)

(3) determine whether the flow is an incompressible flow (5 %)

6. (1) Using scale analysis to derive the two dimensional Prandtl boundary layer equations. (10 %)

(2) Show that the thickness of the boundary layer  $\delta$  is proportional to  $\sqrt{x}$  where x is distance from the leading edge of the plate. (5 %)

7. Explain the following terms (definition and physical interpretation): (20 %)

(1) potential flow and irrotational flow

(2) Kelvin's circulation theorem

(3) barotropic flow and baroclinic flow

(4) circulation and vorticity

(5) gradient and divergence

8. The temperature at a point 50 km north of a station is  $3^\circ\text{C}$  cooler than at the station. If the wind is blowing from the northeast at  $20\text{ ms}^{-1}$  and the air is being heated by radiation at the rate of  $1^\circ\text{C hour}^{-1}$ . What is the local temperature change at the station? (10 %)