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1. A metal sphere of radius R , carrying charge q , is surrounded by a thick concentric metal shell (inner radius a , outer radius b). The shell carries no net charge.
 - (i). Find the surface charge density at R , at a , and at b .
 - (ii). Find the electric field at $r < R$ and $r > b$.
 - (iii). Find the potential at the center, using infinity as a reference point.
 - (iv). Now the outer surface is touched to a grounding wire, which lowers its potential to zero. How do your answers to (i) – (iii) change?

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2. A point charge Q exists at a distance d above an infinite conducting plane which has a nonzero potential V .
 - (i). Determine the electric potential everywhere.
 - (ii). Find the surface charge density on the plane.

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3. Consider a sphere of radius R is rotating about one of its diameters with angular frequency ω .
 - (i). If it has uniform volume charge distribution ρ , determine the magnetic dipole moment.
 - (ii). Find the magnetic field at distance far from the sphere.

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4. Two long coaxial solenoids each carry current I but in opposite directions. The inner solenoid (radius a) has n turns per unit length, and outer one (radius b) has m turns. Find B and H in each of the three regions: (i) inside the inner solenoid, (ii) between them, and (iii) outside both. Evaluate (iv) the mutual inductance and (v) the energy of the system.

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5. Assume an electromagnetic plane wave has the electric field,

$$\vec{E} = E_1 \hat{x} \cos(kz - \omega t) + E_2 \hat{y} \sin(kz - \omega t)$$

where $k = \omega/c$, c is the speed of light and E_1, E_2 are real.

- (i). Determine the polarization of the wave and plot the trace of the tip of \vec{E} in the plane $z=0$.
- (ii). What is the magnetic field of the wave?
- (iii). Calculate the energy density of the wave.