

國立中央大學94學年度碩士班考試入學試題卷 共 2 頁 第 1 頁  
 所別：電機工程學系碩士班丙組 科目：控制系統

1. Given the unity-feedback control system as follows:

$$G(s) = \frac{K(s+1)}{s(s+4)(1+Ts)}$$

Determine the values of  $K$  and  $T$  for stability of this control system. (10%)

2. Design a 3<sup>rd</sup> order controller whose three roots are located at the following locations in the s-plane: -1; -1; -12. The transfer function of the system to be controlled is given by

$$\frac{C(s)}{U(s)} = G(s) = \frac{1}{s(s+1)(s+2)}$$

Determine the controller gain matrix,  $K$ . (20%)

3. Show that the state feedback can cause a loss of observability. (20%)

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4. (i) Plot the root locus of the eq. :  $s^4 + 22s^3 + 40s^2 + ks + k = 0$ .  
(10%)  
(ii) Plot the asymptotes, too.  $(0 \leq k < \infty)$   
(5%)  
(iii) Specify the crossover frequency and the corresponding  $k$ .  
(5%)

5. (i) If  $G(s) = \frac{s^2 + 5s + 6}{s^3 + 9s^2 + 23s + 15}$ , find the controllable canonical form:  $\begin{cases} \dot{x} = Ax + bu \\ y = cx \end{cases}$   
(10%)

- (ii) Is the system in the above observable? Why?  
(5%)

6. Consider a plant described by  
(15%)

$$\ddot{y} + 5\dot{y} + 3y + 2y = u.$$

Assign the states as  $x_1 = y$ ,  $x_2 = \dot{y}$ , and  $x_3 = \ddot{y}$ .

Design  $K = [a \ b \ c]$  so that the characteristic polynomial becomes  $s^3 + 6s^2 + 5s + 8$  after utilizing

$$u = -k \begin{pmatrix} x_1 \\ x_2 \\ x_3 \end{pmatrix}.$$